

Quicksort

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Quicksort

- A more efficient exchange sorting scheme than bubble sort
 - A typical exchange involves elements that are far apart
 - *Fewer interchanges are required to correctly position an element.*
- Quicksort uses a **divide-and-conquer** strategy
 - A recursive approach
 - The original problem partitioned into simpler sub-problems,
 - Each sub problem considered (conquered) **independently**.
- Subdivision continues until sub problems obtained are **simple enough** to be solved directly
 - How simple?

Quicksort: Divide/Split

- Choose some element called a **pivot**
- *Perform a sequence of exchanges* so that
 - All elements that are less than this pivot are to its left.
 - All elements that are greater than the pivot are to its right.
- Divides the (sub)list into two smaller sub lists,
- Each of which may then be sorted independently in the *same* way.

Quicksort

If the list has 0 or 1 elements,

return. *// the list is sorted, simple enough!*

Else do:

↑
Split Pick an element in the list to use as the *pivot*.
↓ Split the remaining elements into two disjoint groups:
 SmallerThanPivot = {all elements \leq *pivot*}
 LargerThanPivot = {all elements $>$ *pivot*}

Return the list rearranged as:

Quicksort(*SmallerThanPivot*),
pivot,
Quicksort(*LargerThanPivot*).

Quicksort Example

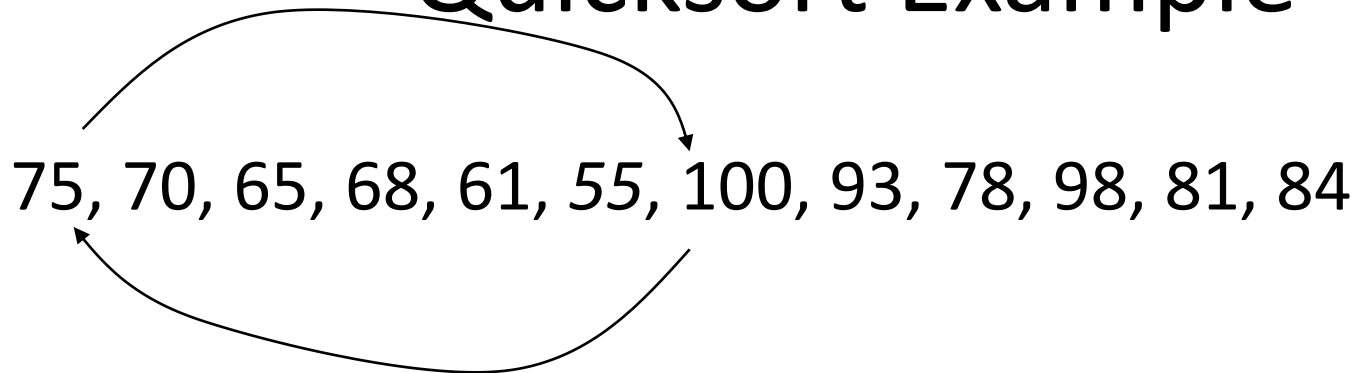
- Given to sort:

75, 70, 65, 84 , 98, 78, 100, 93, 55, 61, 81, 68

- Select, arbitrarily, the first element, 75, as pivot.
- Search from right for elements ≤ 75 , stop at first element ≤ 75
- Search from left for elements > 75 , stop at first element > 75
- Swap these two elements, and then repeat this process

Quicksort Example

75, 70, 65, 68, 61, 55, 100, 93, 78, 98, 81, 84



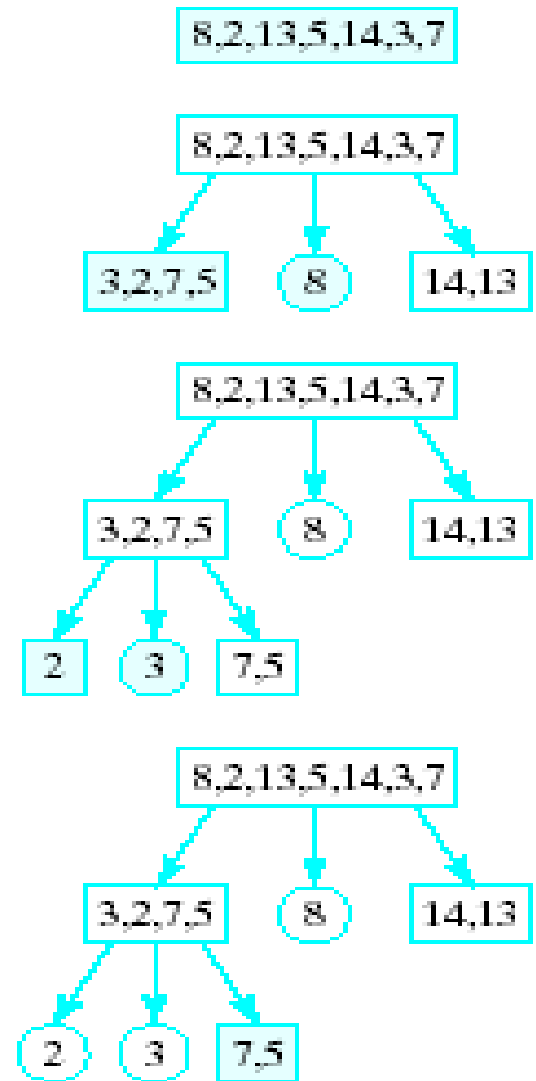
- When done, swap with pivot
- This SPLIT operation placed pivot 75 so that all elements to the left were ≤ 75 and all elements to the right were > 75 .
- 75 is now placed appropriately
- Need to sort sublists on either side of 75

Quicksort Example

- Need to sort (independently):
 55, 70, 65, 68, 61 and
 100, 93, 78, 98, 81, 84
- Let pivot be 55, look from each end for values larger/smaller than 55, swap
- Same for 2nd list, pivot is 100
- Sort the resulting sublists in the same manner until sublist is trivial (size 0 or 1)

Quicksort

- Note visual example of a quicksort on an array



etc. ...

Reflection of Quicksort

- Perform split() operation on a (sub)list, such that: left-sublist, pivot, right-sublist
- Recursively and independently perform split() on left-sublist and right-sublist, until their sizes become 0 or 1 (simple enough).
- So, the basic operation is split!
 - `int split(int x[], int low, int high)`
 - `[low, high]` specifies the sublist.
 - Returns the final position of the pivot

Implementing Quicksort

- Basic operation: split
 - Choose the pivot (e.g., the first element)
 - Scan the (sub)list from both ends, swap elements such that the resulting left sublist $<$ pivot and right sublist \geq pivot
 - `int split (int x[], int first, int last)`

Recursive Quicksort

- `void quicksort(int x[], int n)`

Quicksort: $T(n)$

- Best-case ?
- Worst-case ?

Quicksort Performance

- $O(n \log_2 n)$ is the best case computing time
 - If the pivot results in sublists of approximately the same size.
- $O(n^2)$ worst-case
 - List already ordered, elements in reverse
 - When **Split()** repetitively results, for example, in one empty sublist

Improvements to Quicksort

- An *arbitrary pivot* gives a poor partition for nearly sorted lists (or lists in reverse)
- Virtually all the elements go into either **SmallerThanPivot** or **LargerThanPivot**
 - all through the recursive calls.
- Quicksort takes quadratic time to do essentially nothing at all.

Improvements to Quicksort

- Better method for selecting the pivot is the *median-of-three rule*,
 - Select the median of the first, middle, and last elements in each sublist as the pivot.
- Often the list to be sorted is already partially ordered
- Median-of-three rule will select a pivot closer to the middle of the sublist than will the “first-element” rule.

Improvements to Quicksort

- For small files ($n \leq 20$), quicksort is worse than insertion sort;
 - *small files occur often because of recursion.*
- Use an efficient sort (e.g., insertion sort) for small files.
- Better yet, use **Quicksort()** until sublists are of a small size and then apply an efficient sort like insertion sort.

Non-recursive Quicksort

- Think about non-recursive alg.?