

MATH 2340 WARM-UP PROBLEMS

Consider the differential equation

$$ay'' + by' + cy = 0, \quad y(0) = y_0, \quad y'(0) = y'_0.$$

Match following parameter sets for a, b , and c with the corresponding graph that matches a solution to the initial value problem.

1. Figure A

$$\{a, b, c\} = \{16, 8, 65\} \quad 16y'' + 8y' + 65y = 0 \rightarrow \lambda = -\frac{1}{4} \pm 2i \quad y_1 = e^{-\frac{1}{4}x} \cos(2x)$$

2. Figure E

$$\{a, b, c\} = \{4, 4, 1\} \quad \lambda = -\frac{1}{2} \text{ repeated} \quad y_1 = e^{-\frac{1}{2}x}, \quad y_2 = e^{-\frac{1}{2}x} \cdot x$$

3. Figure F

$$\{a, b, c\} = \{16, 8, -3\} \quad \lambda = -\frac{3}{4}, \quad \lambda = \frac{1}{4}$$

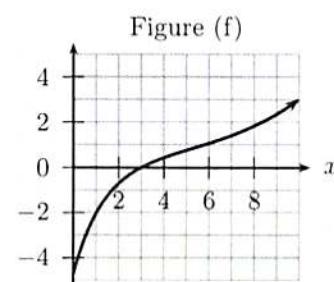
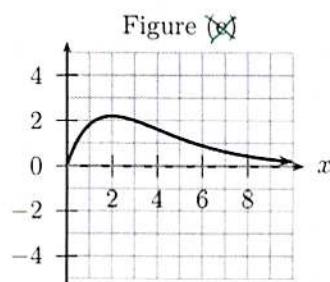
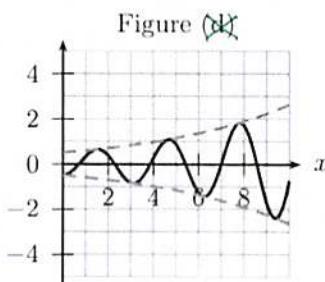
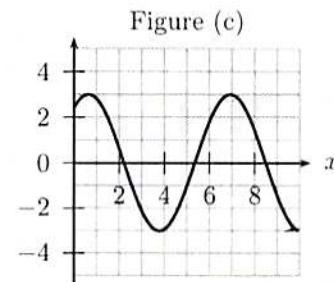
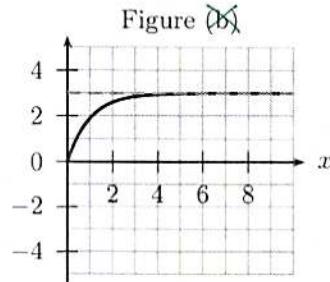
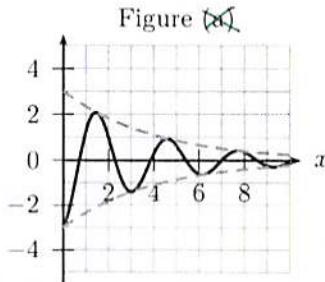
4. Figure B

$$\{a, b, c\} = \{1, 1, 0\} \quad \lambda = 0, \quad \lambda = -1 \quad y_1 = e^{-x}, \quad y_2 = 1$$

5. Figure D

$$\{a, b, c\} = \{16, -8, 65\} \quad \lambda = \frac{1}{4} \pm 2i \quad y_1 = e^{\frac{1}{4}x} \cos(2x), \quad y_2 = e^{\frac{1}{4}x} \sin(2x)$$

exponential decay + oscillation



That's it. No more fun left.